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Automated Classification and Scoring of Smooth Pursuit Eye Movements in Presence of
Fixations and Saccades

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Abstract

Ternary eye movement classification, which separates fixations, saccades, and smooth pursuit from the raw eye positional data, is extremely challenging. This paper develops new and modifies existing eye tracking algorithms for the purpose of conducting meaningful ternary classification. To aid this purpose a set of qualitative and quantitative behavior scores is introduced to facilitate the assessment of classification performance and to provide means for the automated threshold selection. Experimental evaluation of the proposed methods is conducted using eye movement records obtained from 11 subjects at 1000Hz in response to a step-ramp stimulus eliciting fixations, saccades, and smooth pursuits. Results indicate that a simple hybrid method that incorporates velocity and dispersion thresholding allows producing robust classification performance. It is concluded that behavior scores are able to aid automated threshold selection for the algorithms capable of successful classification.

Keywords: Eye movements, classification, algorithm, analysis, scoring, metrics, smooth-pursuit.

INTRODUCTION

The identification of the basic eye movement types from a noisy and frequently inaccurate raw eye positional signal is of utmost importance to the researchers and practitioners that employ eye trackers in their studies. Human oculomotor system (HOS) primarily exhibits six eye movement types: fixations, saccades, smooth pursuits, optokinetic reflex, vestibulo-ocular reflex, and vergence (Leigh & Zee, 2006). Among those eye movement types fixations, saccades, and smooth pursuit are most frequently studied. The following brief definitions can be provided for these eye movement types: eye fixation is an eye movement that keeps an eye gaze stable on selected stationary target, saccade is a very rapid eye rotation moving the eye from one fixation point to the next, smooth pursuit (SP) is eye movement that follows a moving object with a purpose of keeping the object on a high acuity vision zone called the fovea (Duchowski, 2007; Poole & Ball, 2004). Eye fixations are frequently employed for human computer interaction as an input modality (Istance et al., 2010), saccades and smooth pursuits are frequently employed to diagnose pathologies of the HOS or assessing HOS performance in clinical populations (Elina et al., 2009). Therefore, accurate automated classification of eye movements is an important topic of research.

Accurate automated eye movement classification is exceedingly difficult due to the noise and inaccuracies inherited from the eye tracking equipment, dynamics of the HOS behavior, and variability between- and within- eye movement classification algorithms. Variation of single threshold value, in cases when only fixations and saccades are classified, is reported to substantially affect metrics such as number of detected saccades and fixations, average fixation duration and saccade amplitude (Ceballos et al., 2009; Garbutt et al., 2003; Komogortsev et al., 2010; Poole & Ball, 2004). Frequently researchers perform manual classification to avoid miss-

identification issues associated with automated algorithms. However in such cases classification becomes a very long and tedious process. Selection of the thresholds that provide meaningful classification is frequently done empirically with default values suggested by either eye tracking vendors or related literature. Given rapid developments of the eye tracking technologies that vary in hardware, sampling frequencies, and calibration algorithms (Hansen & Qiang, 2010) it is easy to “copy and paste” suggested thresholds; however it is hard to validate classification accuracy. During empirical threshold selection by “eye balling” small part of the classified data it is easy to misclassify some of recordings or misidentify corrective behavior such as corrected undershoots, overshoots, dynamic saccades etc. (Leigh & Zee, 2006).

It is hard to define meaningfulness of the automated classification given a threshold value. For example it is possible to assume that quality of saccade detection can be ultimately judged by such properties as amplitude-duration relationship, main-sequence relationship, and saccades’ waveform¹ (Leigh & Zee, 2006). However, there is a substantial amount of variability for some of those metrics between people (E. Bollen et al., 1993) and even directional differences for the same person (Smit et al., 1990). In this type of circumstances it is very difficult to judge when selected threshold produces accurate performance measured by the above-mentioned metrics, because this performance might depend on multiple factors. Recently, Komogortsev and colleagues have proposed a set of behavior scores with a purpose of selecting a meaningful classification threshold using fixed stimulus (Komogortsev et al., 2010). Behavior scores assume that amount of saccadic and fixational behavior encoded in a simple step-stimulus is matched by the HOS of a normal person therefore providing an opportunity to find a threshold value that en-

¹ An example were saccades are detected based on “the peak-velocity-magnitude-duration parameters” “manually” can be found in (Bahill et al., 1980). However, this manual procedure is obviously very time consuming.

asures such performance. Researchers reported that thresholds selected according to these criteria provided meaningful classification results (Komogortsev et al., 2010).

It should be noted, that the purpose of the scores is not to substitute already established metrics such as amplitude-duration relationship, etc., but to provide an opportunity for the automated selection of the classification parameters immediately after the calibration procedure. In case if experimental stimulus contains step or step-ramp stimulus classification performance for the whole experiment can benchmarked with behavior scores in addition to any other metric employed by the experimenters. The goal of automated threshold selection for a step-ramp stimulus with subsequent employment of the same threshold for dynamic stimuli is particularly attractive because step-ramp stimulus is already presented as a part of the calibration procedure. Recording equipment's performance for a given setup and subject is unlikely to change from calibration to the actual recording. Therefore, it is possible to assume that selected thresholds would continue to provide meaningful classification performance even during presentation of the stimuli that is different from the calibration.

Automated classification of SP in the presence of fixations and saccades is even more difficult task and continues to be a topic of an active research (Agustin, 2009; Larsson, 2010). Most difficult part of ternary eye movement classification is separation between fixations and SP. Two main factors contribute to the challenge: a) a fixation consists of the three sub-movement types such as tremor, drift, and microsaccades. As a result a velocity range during a fixation (velocities up to 30°/s are possible as computed by the main sequence relationship (Leigh & Zee, 2006)) and SP (velocity up to 100°/s is reported in (Carpenter, 1977)) overlap. b) eye tracking noise further blurs quantitative boundaries between fixation and pursuit.

Given the importance of ternary eye movement classification and its challenges it is necessary to find out what degree of meaningful classification can be obtained and if the accuracy of classification performance can be verified by a set of simple behavior scores.

To start answering these questions this work: 1) introduces behavior scores related to SP, 2) proposes an algorithm for ternary eye movement classification 3) evaluates automated and manual ternary classification based on the proposed scores, and 4) establishes automated selection of the classification thresholds based on the ideal values of behavior scores.

OVERVIEW

Classification of Fixations and Saccades

In general eye movement classification algorithms consider different properties of the signal that is captured by an eye tracker. In case when fixations have to be separated from saccades classification algorithms can be broken into the following groups: 1) position-based – Dispersion Threshold Identification (I-DT), Minimum Spanning Tree Identification (I-MST), 2) velocity-based - Velocity Threshold Identification (I-VT), Hidden Markov Model Identification (I-HMM), Kalman Filter Identification (I-KF), 3) acceleration-based – Finite Input Response Filter Identification (I-FIR) (Komogortsev et al., 2010; Salvucci & Goldberg, 2000; Tole & Young, 1981). To the best of our knowledge these algorithms have not been “successfully” applied to the problem of ternary classification.

Human Visual System Performance during Pursuit Stimuli

The SP movement consists of the three phases: initiation, steady-state, and termination (Leigh & Zee, 2006; Mohrmann & Thier, 1995; Robinson, 1965; Terry Bahill & McDonald, 1983). The initiation phase can be broken into three steps: 1) the SP latency when the brain programs the movement, 2) the initial SP represented by an exponential rise in the eye movement

velocity, 3) corrective saccade that brings the target closer to the fovea. The steady-state consists of continuous SP movement that might be interspersed by the corrective saccades. The termination phase consists of three steps 1) the response latency, 2) an exponential decay in velocity, 3) an optional corrective saccade(s) that bring the eye to a new target.

It is possible to assume that separation of the steady-state SP from the fixation signal is simple via a velocity threshold, however following factors challenge accurate classification.

The first factor is jitter during fixations. Jitter is frequently caused by the inaccuracies in the eye tracker's gaze position estimation. Good eye-tracker's positional accuracy performance is varied in the range of 0.25-1°.

The second factor is presence of miniature eye movements such as drift, micro-saccades, and tremor (Leigh & Zee, 2006) which result in high spread of the amplitudes for the positional (e.g., up to 1.5°) and velocity (e.g., up to 40°/s) signal. This spread does not greatly impact classification accuracy if only fixations and saccades are present, however in cases of low velocity SP (e.g. 20-40°/s) the results of classification might be poor.

The third factor is variability of the eye movement behavior among people and its dependence on the task. For example, response times can be different for “Express Saccade” makers and naïve subjects in a gap-step-ramp experiments (Kimmig et al., 2002). Also humans are capable of matching velocities of up to 90°/s during SP exhibited to ramp stimulus with constant velocity (Meyer et al., 1985). For unpredictable motion it has been suggested that humans cannot pursue small targets at speeds faster than 40°/s (Young & Stark, 1963).

Existing Algorithms for Automated Classification of Smooth Pursuit

In the previous research the separation of SP was done in cases when only SP and saccades were present. For example a single threshold-based algorithm was employed by (Bahill et

al., 1980). The researchers used a velocity threshold of 50°/s to separate saccades from SP. All sequences of samples with velocity greater than threshold were checked upon matching main-sequence relationships. If a sequence of points met these criteria than all its samples were marked as a saccade. Otherwise the samples were discarded. Bahill was able to use main sequence relationship as a criterion for meaningful classification because only horizontal saccades were considered.

For ternary classification an interesting approach was proposed by San Agustin (2009) and further enhanced by Larsson (2010). The approach monitors the direction of movement and the rate of movement to separate fixations from SP. This approach together with a new proposed approach is discussed in the section describing the classification algorithms.

BEHAVIOR SCORES FOR SMOOTH PURSUIT CLASSIFICATION

Considering the multitude of factors affecting SP performance and especially between-subject variability, it is important to develop simple metrics that can assess automated eye movement classification performance against ramp stimulus with constant velocity, signaling the cases of classification success or failures with an ultimate goal of suggesting parameters/thresholds for meaningful classification even in cases of unpredictable SP-exhibiting content.

Previously Komogortsev et al. (2010) created a set of behavior scores that allowed assessment of classification quality or even determining the optimal threshold values when only fixations and saccades are present. This work continues in the same direction fine-tuning already existing scores and creating additional scores to assess meaningfulness of ternary classification. For the purposes of the initial assessment, behavior scores assume that the amount of fixational,

saccadic, and SP behavior encoded in step and ramp stimuli is matched by the HOS in a normal subject.

Scores when only fixations and saccades are present

Komogortsev et al. (2010) originally proposed three behavior scores namely Fixation Quantitative Score (FQnS), Fixation Qualitative Score (FQIS), and Saccade Quantitative Score (SQnS). The scores were originally designed to measure classification quality if only fixations and saccades are present in the raw eye positional trace. We perform following additions and modifications that allow extending the utility of behavior scores for ternary classification.

Modified Saccade Quantitative Score

The SQnS measures the amount of saccadic behavior in response to a stimulus. The SQnS is defined as the ratio of all detected saccade amplitudes to all saccade amplitudes encoded in the stimulus (Komogortsev et al., 2010). To avoid counting corrective saccades during SP the SQnS is modified to consider saccades that directly correspond only to the stimulus-saccades represented by the instantaneous jump of the target's location. To attain this goal a temporal window is introduced which considers saccades in response to the step part of the stimulus only. This is achieved by a use of a temporal window that monitors the eye positional signal in a fixed time interval prior and after stimulus change. This logic allows correctly considering anticipatory saccades and corrective saccades for the SQnS computation.

The ideal SQnS score, which is only achieved if the HOS perfectly executes a saccade within the temporal window and classifier accurately detects it, is 100%. In practice the SQnS value might be lower because of some amount of the anticipatory and the corrective saccadic behavior that might fall outside of the temporal window.

Modified Ideal Fixation Quantitative Score

The FQnS measures the amount of fixational behavior in response to a stimulus. The FQnS is defined as the amount eye position points, that are part of the fixation related to stimulus-fixation², divided by total number of stimulus-fixation points (Komogortsev et al., 2010). The ideal FQnS score presented in (Komogortsev et al., 2010) did not consider the effect of SP on score computation, therefore, in this work we provide a modified formula that accounts for SP effects.

$$\text{Ideal_FQnS} = 100 \left(1 - \frac{mS_l + kP_l + \sum_{j=1}^m D_{\text{sac_dur}_j}}{\sum_{i=1}^n D_{\text{stim_fix_dur}_i}} \right) \quad 1$$

where n is the number of stimulus fixations, $D_{\text{stim_fix_dur}_i}$ is duration of the i th stimulus fixation, S_l is saccadic latency, m is the number of stimulus transitions between fixations and saccades, $D_{\text{sac_dur}_j}$ is the expected duration of a saccade in response to the stimulus saccade j , k is the number of stimulus transitions from SP to fixations, and P_l is the duration of the SP termination phase during fixation-stimulus.

Smooth Pursuit Qualitative Scores

The intuitive idea behind the Smooth Pursuit Qualitative Scores (PQIS) is to compare the proximity of the detected SP signal to the signal presented in the stimuli. Two scores are indicative of the positional (PQIS_P) and the velocity (PQIS_V) accuracy.

² For the simplicity of writing we use following definitions that describe stimulus signal behavior: stimulus-saccade – step part of the stimulus signal that elicits eye saccades, stimulus-SP – ramp part of the signal that elicits eye SP, stimulus-fixation – flat part of the stimulus signal that elicits eye fixations. Eye fixation, saccade, and SP are called simply fixation, saccade, and SP, without any prefix.

The PQIS_P and PQIS_V calculations are similar to the FQnS (Komogortsev et al., 2010), i.e. for every SP point (x_s, y_s) of the presented stimuli, the check is made for the point in the eye position trace (x_e, y_e) . If such point is classified as part of SP, the Euclidean distance between these two points and the difference between their speeds are computed. Then the sum of such distances and speed differences are normalized by the amount of points compared.

$$PQIS_P = \frac{1}{N} \cdot \sum_{i=1}^N \text{pursuit_distance}_i \quad 2$$

$$PQIS_V = \frac{1}{N} \cdot \sum_{i=1}^N \text{pursuit_speed_difference}_i \quad 3$$

N is the amount of stimuli position points where stimulus-SP is matched with corresponding eye position sample detected as SP. $\text{pursuit_distance}_i = \sqrt{(x_s^i - x_e^i)^2 + (y_s^i - y_e^i)^2}$ and represents the distance between stimuli-SP position and the corresponding SP point. $\text{pursuit_speed_difference}_i = |v_s^i - v_e^i|$ and represent the difference between speeds in i -th stimuli point and corresponding point in the raw eye positional sequence.

Ideal PQIS scores, which can only be achieved if HOS perfectly matches positional/velocity characteristics of the moving target and no calibration errors are present, are $PQIS_P=0^\circ$ and $PQIS_V=0\%/s$. In practice ideal scores might not be achieved due to calibration errors, corrective behavior, and classification inaccuracies.

It should be noted that qualitative scores are indicative of two things: 1) how well the HOS follows the target, 2) how accurately the tracking equipment works for a given participant. Considering this we did not use the existing SP gain metric, defined as peak eye velocity/peak target velocity (Leigh & Zee, 2006), due to the fact that SP gain is designed to measure the HOS performance only.

Smooth Pursuit Quantitative Score

Smooth Pursuit Quantitative Score (PQnS) measures the amount of detected SP behavior given the SP behavior encoded in the stimuli. To calculate PQnS two separate quantities are computed. One measures the total length of the SP trajectories presented by the stimuli. The second one measures the overall length of the properly detected SP by the classifier. The ratio of these two values defines the score.

$$PQnS = 100 \cdot \frac{total_detected_SP_length}{total_stimuli_SP_length} \quad 4$$

The computation of the ideal PQnS can be performed as:

$$Ideal_PQnS = 100 \cdot \left(1 - \frac{n \cdot P_l + \sum_{j=1}^n D_{cor_sac_dur_j}}{\sum_{i=1}^n D_{stim_pur_dur_i}} \right) \quad 5$$

where n is the number of stimulus-pursuits, $D_{stim_pur_dur_i}$ is duration of the i^{th} stimulus-pursuit, P_l is pursuit's latency prior to the onset of the corrective saccade that brings the fovea to the target, and $D_{cor_sac_dur_j}$ is the expected duration of the corrective saccade. The Ideal_PQnS assumes that the HOS exhibits the SP for the duration of the target's movement immediately after the initial corrective saccade. Subsequently, accurate SP classification has to be performed for the duration of the movement. In practice ideal score might not be achieved due to the classification errors or additional corrective saccades occurring during the SP-stimulus.

Misclassified Fixation Score (MisFix)

Misclassification error of the SP can be determined during a fixation stimulus, when correct classification is most challenging. $SP_fixation_points$ is the number of points in eye position trace that were classified as SP but the corresponding stimuli point for them is a fixation. $total_stimuli_fixation_points$ is the total number of fixation points in stimuli. To calculate MisFix, two separate quantities are calculated. $SP_fixation_points$ is the number of points in the eye posi-

tion trace that were classified as SP but the corresponding stimuli point for them is fixation. *total_stimuli_fixation_points* is the total number of fixation points in stimuli

$$\text{MisFix} = 100 \cdot \frac{SP_fixation_points}{total_stimuli_fixation_points} \quad 6$$

Computation of the ideal MisFix should take into the consideration the fact that termination phase of SP continues during fixational stimulus after the SP stimulus is over. Therefore, following formulation is employed for the computation of the ideal MisFix score.

$$\text{Ideal_MisFix} = 100 \cdot \left(\frac{n \cdot P_{lt} + \sum_{j=1}^n D_{cor_sac_dur_j}}{\sum_{i=1}^n D_{stim_fix_dur_i}} \right) \quad 7$$

where n is the number of SP present in the stimuli, average duration of the latency of the termination phase P_{lt} prior to the last corrective saccade leading to fixational stimulus position. $D_{cor_sac_dur_j}$ is duration of the corrective saccade, if present. In calculation of the Ideal_MisFix we assumed that each stimulus SP is followed by stimulus fixation.

ALGORITHMS FOR SMOOTH PURSUITS DETECTION

Velocity and Velocity Threshold Identification (I-VVT)

We modify the I-VT algorithm to perform ternary classification. For the purposes of separating SP from fixations a second velocity threshold is introduced. To highlight such modification the algorithm's name is changed to the (Velocity and Velocity Threshold Identification) I-VVT. Figure 1 presents the pseudocode. The pseudocode contains Filter Function that accepts a list of the pre-classified saccades for the purpose of filtering noisy saccade-like events according to minimum amplitude and duration. In case of this work such events with amplitudes of less than 3.5° and 4 ms. in duration were discarded. "Filter Function" sub-section in the "Discussion" provides additional description on the topic of filtering.

The I-VVT algorithm is capable of real-time performance, however it is not able to provide accurate classification as discussed in the results section.

Note that our implementation of each algorithm presented here and behavior scores together with eye movement recordings can be downloaded here (Komogortsev, 2011).

Velocity and Movement Pattern Identification (I-VMP)

We call the approach proposed by Agustin (2009) and enhanced by Larsson (2010) Velocity and Movement Pattern Identification (I-VMP), because it employs velocity threshold to first identify saccades similarly to I-VVT.

Subsequently, it analyses the movement patterns to separate SP from fixations. The movement pattern is analyzed in a temporal window with a size of T_w . In that window the magnitude of movement is computed by analyzing angles created by every pair of the adjacent positional points and the horizontal coordinate axis. Once the value representing the magnitude of movement is computed it is compared against a threshold T_m . Values above the threshold are marked as SP and below the threshold are marked as fixations. Figure 2 presents the pseudocode. More detailed description of the algorithm is provided elsewhere (Larsson, 2010).

Algorithm: *Smooth Pursuit Classification (I-VVT)*

Input: array of eye position points, saccade velocity threshold - T_{vs} , smooth pursuit velocity threshold - T_{vp}

Output: list of fixations, saccades, and smooth pursuits

Calculate point-to-point velocities for each point

Mark all points above T_{vs} as saccades

Mark all unclassified points below T_{vp} as fixations

Mark all unclassified points as smooth pursuit

Filter Function (array of pre classified saccades)

Merge Function(array of pre classified smooth pursuits, fixations, and saccades)

Merge every group of consecutive saccade points into a saccade with identified onset, offset, and amplitude.

Merge every group of fixation points into a fixation with identified centroid coordinates, onset, and duration.

Merge every group of smooth pursuit points into a smooth pursuit with identified onset, offset, and trajectory.

Return saccades, fixations, and smooth pursuits

Figure 1. Pseudocode for Velocity and Velocity Threshold Identification algorithm.

Velocity and Dispersion Threshold Identification (I-VDT)

In this work we propose a ternary classification algorithm called Velocity and Dispersion Threshold Identification (I-VDT). It performs the initial separation of saccades similarly to the I-VVT and the I-VMP. Subsequently, it separates SP from fixations by employing a modified dispersion threshold identification method, which within a temporal window of the size T_w monitors dispersion of the points (corresponding threshold is T_d). Figure 3 presents the pseudocode. Dispersion of the points is computed in the same way as presented in (Salvucci & Goldberg, 2000).

Algorithm: *Smooth Pursuit Classification (I-VMP)*
Input: array of eye position points, saccade velocity threshold - T_v , temporal window size - T_w , movement threshold - T_M
Output: array of fixations, saccades, and smooth pursuits

Calculate point-to-point velocities for each point
Mark all points above T_v as saccades

Filter Function (array of pre classified saccades)

While temporal window T_w does not reach the end of array

Mark all unclassified points inside T_w as fixations

For all pairs of adjacent points inside of T_w calculate an angle created by the pair and horizontal axis

Represent computed angles as points on circumference of a unit circle

Calculate mean (M_x, M_y) of x and y coordinates of those points)

If (distance between (M_x, M_y) and (0,0) > T_M)

Mark fixation points inside the T_w as smooth pursuit

End if

End while

Merge Function(array of pre classified smooth pursuits, fixations, and saccades)

Return saccades, fixations, and smooth pursuits

Figure 2. Pseudocode for Velocity and Movement Pattern Identification algorithm.

EXPERIMENTAL SETUP

Apparatus

The data was recorded using the EyeLink 1000 eye tracker (EyeLink, 2010) at 1000Hz on a 21 inch CRT monitor with a screen resolution of 1024x768pix and refresh rate of 80Hz. Vendor reported spatial resolution for EyeLink 1000 is 0.01° (EyeLink, 2010). To ensure high accuracy of the eye movement recording a chin rest was employed. The chin rest was positioned at 70cm in front of the monitor. The recordings were performed in the monocular mode for the eye that provided the best calibration accuracy. The height of the chin rest was adjusted to ensure

that primary position of the recorded eye corresponded to the center of the screen. The stimulus screen was rectangular to the line of view. Recorded raw eye positional signal was first processed by heuristic one-sample filter described in (Stampe, 1993) and as implemented by EyeLink 1000 vendor. The raw eye positional signal was subsequently translated to the coordinates presented in the degrees of visual angle with the center of coordinate system corresponding to the center of the screen. The procedure of converting the signal from the eye tracking units to the degrees of the visual angle is described elsewhere (Duchowski, 2007).

Stimulus signal

2D step-ramp stimulus was presented by moving target. Presented range of stimulus-saccades' amplitudes was 14.2-28.5° (M=20.2, SD=6.7). Presented range of stimulus-SPs' velocities was 20.1-53.7°/s (M=38.0, SD=11.3). Stimulus-SP velocity was constant at each interval. Only single target was continuously presented throughout the experiment. Total stimulus duration was approximately 35 sec. Detailed target's behavior is described in Table 1 and is supplied as an additional video file attached to this submission. The target was presented as a white dot

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Algorithm: Smooth Pursuit Classification (I-VDT)
Input: array of eye position points, velocity threshold -  $T_V$ , dispersion threshold -  $T_D$ , temporal window size -  $T_W$ 
Output: array of fixations, saccades, and smooth pursuits

Calculate point-to-point velocities for each point
Mark all points above  $T_V$  as saccades

Filter Function ( array of pre classified saccades )
Initialize temporal window over first points in the remaining eye movement trace
While temporal window does not reach the end of array
    Calculate dispersion of points in window
    If (dispersion <  $T_D$ )
        While dispersion <  $T_D$ 
            Add one more unclassified point to window
            Calculate dispersion of points in window
        End while
        Mark the points inside of the window as fixations
        Clear window
    Else
        Remove first point from window
        Mark first point as a smooth pursuit
    End if
End while

Merge Function(array of pre classified smooth pursuits, fixations, and saccades)
Return saccades, fixations, and smooth pursuits
    
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Figure 3. Pseudocode for Velocity and Dispersion Threshold Identification algorithm.

with a size of approximately 1° in diameter and the center marked with a small black dot to facilitate higher targeting accuracy for HOS. Remaining screen's background was black.

The data recorded for the above-described task was a part of a larger study that had its purpose in establishing a normal baseline among healthy subjects for subsequent comparison of data with people who had mTBI injuries. Specifically, task described here was presented as the last stimulus in a battery of other eight step and ramp stimuli tasks. Each task in this sequence was preceded by calibration and calibration verification procedure. The battery of tasks was designed under a guidance of Physical Therapist with one of the goals

to prevent excessive fatigue as part of the task completion. Specifically, in that sequence one-minute break (or longer by request) was given to subjects between each individual tasks. The duration of the whole experiment for each participant on average was approximately 25 minutes.

Onset time, ms	Length, ms	Stimulus onset coordinates, deg		Stimulus Signal	
		X	Y	A	V
1000	709	0	0.00	14.2°	20.1°/s
2709	606	-10	10.15	14.2°	23.5°/s
4314	-	0	0.00	14.2°	-
5314	-	-10	10.15	14.2°	-
6315	531	0	0.00	14.2°	26.8°/s
7846	471	-10	-10.16	14.2°	30.2°/s
9316	-	0	0.00	14.2°	-
10316	-	-10	-10.16	14.2°	-
11317	425	0	0.00	14.2°	33.5°/s
12742	386	10	-10.16	14.2°	36.9°/s
14127	-	0	0.00	14.2°	-
15127	-	10	-10.16	14.2°	-
16128	353	0	0.00	14.2°	40.3°/s
17481	653	10	10.15	28.5°	43.6°/s
19134	607	-10	-10.16	28.5°	46.9°/s
20740	-	10	10.15	28.5°	-
21740	-	-10	-10.16	28.5°	-
22741	400	10	10.15	20.0°	50.0°/s
24141	566	-10	10.15	28.5°	50.3°/s
25707	531	10	-10.16	28.5°	53.6°/s
27237	-	-10	10.15	28.5°	-
28237	-	10	-10.16	28.5°	-
29237	-	-10	10.15	28.5°	-
31237	-	10	-10.16	20.3°	-
32237	-	10	10.15	20.0°	-
33237	-	-10	10.15	14.2°	-

Table 1. Presented step-ramp stimulus characteristics. Ramp characteristics are highlighted with grey. Step characteristics are described by the remaining rows. Value A presents the amplitude of the target's jump (step stimulus) for saccades or distance traveled for the SP eliciting target (ramp stimulus). Value V represents the velocity of target's movement during ramp stimulus. Within each single time interval velocity value was a constant. Target was stationary between step and ramp signal, therefore invoking eye fixations.

Participants & Recordings

The test data consisted of a heterogeneous subject pool, age 18-25, with normal or corrected-to-normal vision. A total of 11 participants volunteered for the evaluation test. None of the participants had prior experience with eye tracking. The mean percentage of invalid data was 1.24% with maximum 7.61%. All recordings were employed during automated classification assessment. Only three recordings selected by criteria described next were employed during manual assessment.

Manual Classification

Manual classification was performed by a post-doctoral researcher to establish performance baseline and was done by a visual inspection of the recorded data where raw positional coordinates were converted to the coordinates in degrees of the visual angle as described in the “Apparatus” subsection. The process of visual inspection consisted of examining the horizontal, vertical components of movement and in most difficult cases 3D view of the signal (Komogortsev, 2011). Saccades were separated when the signal’s positional change was large. Fixations were separated when the signal stayed within a certain positional proximity with jitter, tremor and micro saccades present in the signal. Smooth pursuit was characterized as a signal with very low jitter and continuous directional change of the eye-gaze position. Initial corrective saccades in response to the onset of stimulus-SP were classified as saccades.

Due to considerable time necessary to classify signal manually (approximately 2.5 hours per recording) only three records were classified manually and were labeled as “good”, “medium”, and “bad”. Please note that “good”, “medium”, “bad” categorization contains the description of quality of signal as recorded by the eye tracking equipment and the quality of the HOS for matching stimulus behavior. Next we have provided qualitative description of the recorded sig-

nal for each category, however, the process of manual classification and categorization can be considered as subjective. “Good” (Subject 7) was selected due to low jitter (approximate average amplitude of 0.2° during fixations), lack of large saccade overshoots/undershoots due to initial accurate saccade in response to the step signal change (the amplitude of the correctional behavior did not exceed 1.5°), and close match of SP to the stimulus-SP position (corrective saccade during SP are infrequent and small in amplitude, i.e., $1-3^\circ$). “Medium” (Subject 1) recording had higher jitter (amplitude range $0.3-1.5^\circ$), corrective saccades to compensate for the initial overshoots/undershoots in response to the step signal change are large (amplitude range $3-4^\circ$), ramp signal was not well matched by the HOS (more frequent corrective saccades with larger amplitudes, e.g., $1.5-4^\circ$). “Bad” (Subject 10) was selected due to high jitter (amplitude range $1.5-2^\circ$), prolonged corrective behavior during the fixational stimulus that consisted of sequence of corrective saccades and drifts, pure matching of ramp signal by the HOS (all corrective saccades had amplitudes higher than 2°).

Ideal Scores: To compute the Ideal_FQnS by the eq. (1) for the stimulus described by Table 1 following assumptions are made: average saccade latency is 200 ms., saccade duration is computed by the eq. (3) in (Komogortsev et al., 2010), average duration of the SP termination phase is 130 ms. As a result computed Ideal_FQnS is 83.9%. To compute the Ideal_PQnS by the eq. (5) following assumption is made after manual inspection of the recorded data: SP latency for stimulus-pursuits with velocity $<20^\circ/s$ is 0 ms, $<30^\circ/s$ is 230ms, $<40^\circ/s$ is 210ms, $<50^\circ/s$ is 180, and $>50^\circ/s$ is 210ms. Latency numbers estimated here already contain the duration of the initial corrective saccade. As a result computed Ideal_PQnS is 52%. Average latency duration in termination phase is 153 ms. for our data. Therefore, Ideal_MisFix is computed to be approxi-

mately 7.1%. Latency number estimated here already contains the duration of the final corrective saccade.

RESULTS

Manual Classification

Evaluated Quality	Good	Medium	Bad		
Score/Subject	S7	S1	S10	Average	Ideal Scores
SQnS	96%	84%	89%	90%	100%
FQnS	71%	63%	42%	56%	84%
PQnS	39%	47%	40%	42%	52%
MisFix	6%	13%	33%	17%	7.1%
FQIS	0.44°	0.46°	0.58°	0.49°	0°
PQIS_P	3.15°	3.07°	2.58°	2.93°	0°
PQIS_V	23°/s	39°/s	30°/s	31°/s	0°/s

Table. 2 Manual classification results and ideal behavior scores.

Table 2 presents the behavior scores computed for manually classified data and Figure 6 presents an example of manually classified data. The FQnS had the closest value to the ideal score of 71%. The SQnS was lower than the ideal score of 100%, however the difference was not substantial, i.e., average SQnS computed as a result of manual classification was 90%. The PQnS value was lower than the ideal value of 52%, however the difference was not large, i.e., average PQnS computed as a result of manual classification was 42%. This result can be attributed to the fact that frequently HOS exhibits corrective saccade interspersed by fixations to follow ramp stimuli. Such corrective saccades lower the PQnS value. The average MisFix was higher than the ideal number of 7.1%, due to the variations in the SP termination phase and misclassification errors, however for the record marked as “good” the MisFix was almost the same as the ideal number. All behavior qualitative scores present reasonable values indicating relatively small positional and velocity errors between presented stimulus and recorded eye movements.

Automated Classification

Velocity threshold that separates saccades from fixations and SP was set to 70°/s for all classification algorithms considered in this work. Such threshold was selected following the recommendations presented in (Komogortsev et al., 2010) allowing fixing the saccade classification performance and investigating the performance of the most challenging part of the classification,

i.e., separation of SP from fixations. Resulting SQnS was 92% for all classification algorithms which is quite close to the ideal score of 100% discussed in (Komogortsev et al., 2010) and to the results of the manual classification.

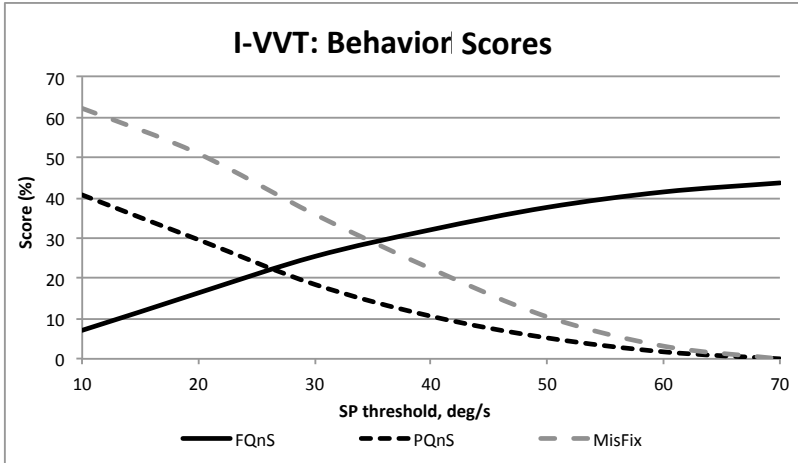


Figure 4. Behavior scores for the I-VVT. x axis – represents the value of SP threshold (T_{vp}). y – axis represents score(s) value.

I-VVT: Figure 4 presents behavior scores. The FQnS starts extremely low and increases together with the value of the SP threshold. The PQnS score starts at 41% and decreases. The MisFix starts high and decreases to 0% when SP threshold reaches saccade threshold. Increase of the FQnS and parallel decrease of the PQnS depicts classification failure of the I-VVT, which is represented by the impossibility of accurately classifying both fixations and SP at the same time. The intersection point at SP threshold of 26°/s yields FQnS=PQnS=22% is far from the values provided by manual classification. At the same time mismatch scores are too high.

I-VMP: Figure 5 presents the behavior scores. The values of the FQnS and the PQnS immediately indicate that magnitude of movement threshold T_m with values of 0.1 and 0.4 does not yield acceptable classification performance, i.e., in case of $T_m=0.1$ the FQnS is too low and the PQnS is too high and in case of $T_m=0.4$ the FQnS is too high and the PQnS is too low. The threshold value of $T_m=0.2$ provides the most usable case, where the FQnS slightly grows, when temporal window size increases, and essentially reaches the value of 63%. The PQnS slightly decreases eventually reaching the value of 49% and stabilizing at that value starting temporal

window threshold of $T_w=120\text{ms}$. Obtained quantitative scores are not far from the average values depicted by the Table 2. Mismatch score (MisFix) starts with relatively high value but decreases with the increase of the temporal window. Score value stabilizes and becomes close to the average depicted by Table 2 after the temporal window reaches 120ms. The FQIS does not exceed 1.1° . The PQIS_V remains relatively stable at 58%. The PQIS_P fluctuates at approximately 3.4° .

I-VDT: Figure 5 presents classification performance of the I-VDT algorithm. Impact of two factors on the I-VDT performance is investigated: dispersion threshold and the size of the temporal window. The increase in dispersion threshold increases the FQnS, however slightly yielding maximum at 82%. The increase in dispersion threshold T_d significantly decreases the PQnS. At $T_d=1.5^\circ$ the PQnS almost reaches 53%, while at $T_d=2.5^\circ$ the PQnS only reaches 37%. The size of the temporal window does not impact the FQnS, however the growth in the temporal window size produces substantial growth in the PQnS. The PQnS starts saturating at window sizes exceeding 110ms. Eventually, obtained quantitative scores are not far from the average values depicted by the Table 2. MisFix is higher for smaller dispersions. The growth of the temporal window makes MisFix grow slowly, essentially, reaching the value obtained by the manual classification (Table 2). Qualitative scores with the exception of the PQnS_V are not affected either by the dispersion threshold or the temporal window size. The velocity error represented by the PQnS_V goes down when temporal window size is increased. PQnS_V value is saturated after the temporal window size reaches 110ms. Smaller dispersion value yields smaller PQnS_V value. The FQIS stays below 0.75° for all threshold and temporal window sizes.

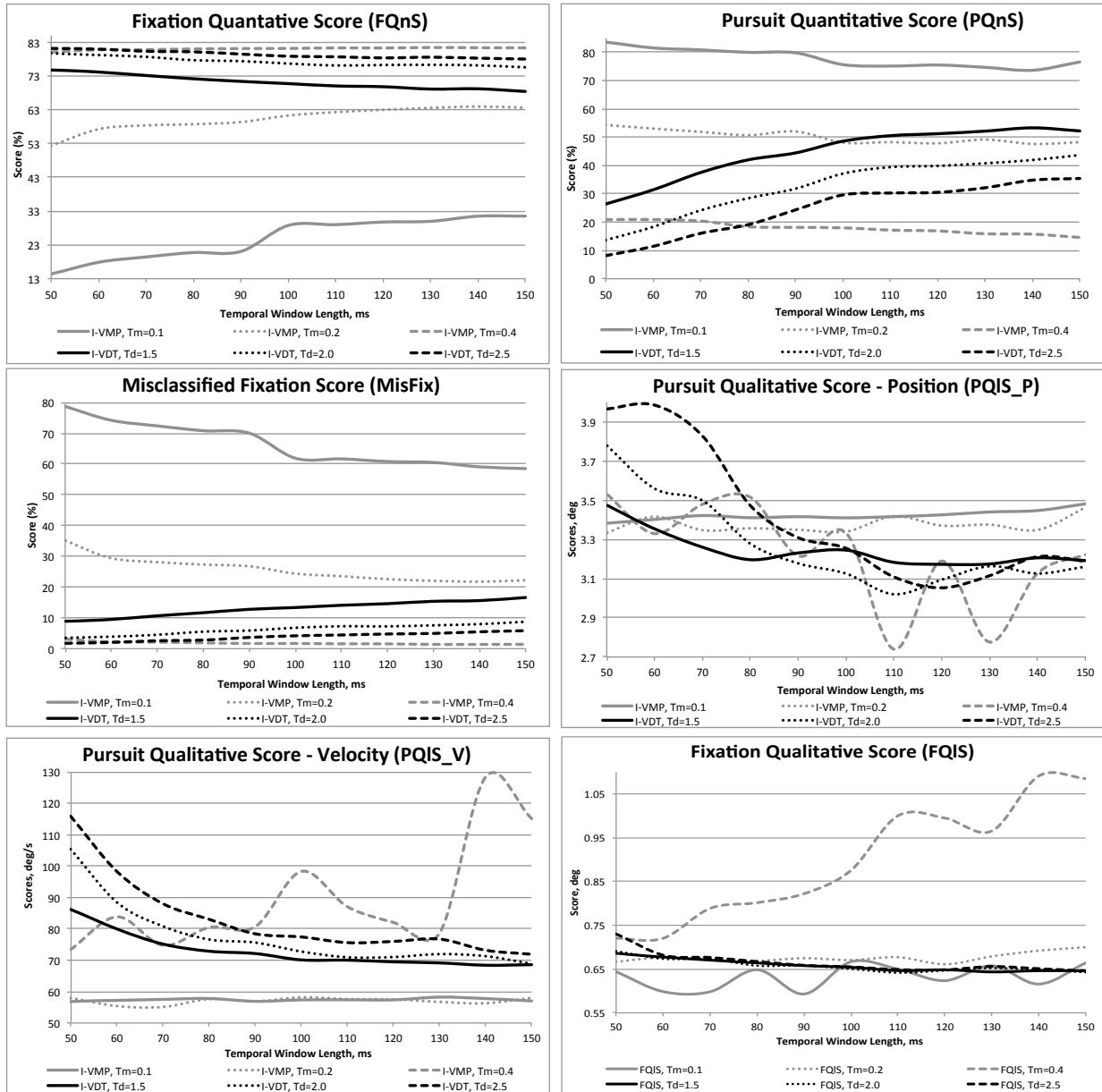


Figure 5. Behavior scores for the I-VMP & the I-VDT. x axis – represents the size of the temporal sampling window. y – axis represents score(s) value.

I-VDT vs. I-VMP: From our experimentation we conclude that the performance of the I-VDT is less impacted by the thresholds than the performance of the I-VMP. If the optimum thresholds are selected for the I-VMP classification performance becomes very similar to the I-VDT, however qualitative scores (FQIS, PQnS_V, PQnS_P) and MisFix are slightly better for the I-VDT when most usable thresholds are considered.

DISCUSSION

Manual Selection of Meaningful Thresholds

Based on the results of classifications presented by Figures 4-5 we can manually select classification thresholds that provide best classification performance for each algorithm. Please note that saccade related threshold is fixed to 70°/s for all algorithms during manual classification.

For the **I-VVT** the optimal values of fixation threshold is 26°/s for which more or less balanced performance is achieved. However, this optimal point produces low qualitative scores and high mismatch scores when compared to the average values presented by Table 2.

For the **I-VMP** the optimal value of the magnitude of movement threshold is $T_M=0.2$, with a temporal window range between the 120-140 ms. Such thresholds produce the scores that are close to the average values depicted by the Table 2.

For the **I-VDT** the optimal dispersion threshold is $T_D=2^\circ$, with the temporal window of 110-150 ms. These thresholds allow to obtain scores that are close to the average scores presented by the Table 2. An example of the raw eye positional signal classified by above-mentioned thresholds is depicted by Figure 7.

Automated Selection of Meaningful Thresholds based on the Ideal Behavior Scores

In this section we investigate the feasibility of automated selection of classification thresholds based on the values of the ideal behavior scores. The idea is to select classification threshold values that allow minimizing the difference between actual and the ideal values of the behavior scores. For this purpose following objective function is selected for the minimization process:

$$F(T_1, T_2, \dots, T_i) = \sqrt{(\text{Ideal_SQnS} - \text{SQnS})^2 + (\text{Ideal_FQnS} - \text{FQnS})^2 + (\text{Ideal_PQnS} - \text{PQnS})^2} \quad 7$$

where T_1, T_2, \dots, T_i thresholds employed for the identification and SQnS, FQnS, PQnS actual behavior scores that are achieved for given thresholds.

We have employed The Nelder-Mead (NM) simplex algorithm (Lagarias et al., 1998) (fminsearch implementation in MATLAB) with an objective function presented by the eq. 7 to select optimal threshold values.

For the **I-VVT** the optimal velocity threshold for saccades is $T_{V_s}=90^\circ/\text{s}$, the optimal velocity threshold for SP is $T_{V_p}=50^\circ/\text{s}$. These thresholds allow to obtain following behavior scores: SQnS=93.1%, FQnS=40.3%, PQnS=11.4%, MisFix=22.4%.

For the **I-VMP** the optimal velocity threshold is $T_v=90^\circ/\text{s}$, dispersion threshold is $T_D=2.5^\circ$, with the temporal window of $T_w=80$ ms. These thresholds allow to obtain following behavior scores: SQnS=90.4%, FQnS=68.9%, PQnS=44.3%, MisFix=15.9%.

For the **I-VDT** the optimal velocity threshold is $T_v=75^\circ/\text{s}$, dispersion threshold is $T_D=1.9^\circ$, with the temporal window of $T_w=150$ ms. These thresholds allow to obtain following behavior scores: SQnS=91.6%, FQnS=74.95%, PQnS=46.07%, MisFix=9.4%. An example of the raw eye positional signal classified by above-mentioned thresholds is depicted by Figure 8.

Manual vs. Automated Selection of Classification Thresholds

There is little difference (e.g., Figure 7 vs. Figure 8) when classification thresholds are selected manually based on the overall picture of the classified data (e.g., Figure 5) and fully automated approach based on the proposed objective function (eq. (7)). Practically, automated threshold selection might be preferable, due to the reduced burden on the facilitator and reasonable outcome of the classification performance.

Variability of HOS Performance

During manual inspection of the recorded data we have noticed substantial variability of the HOS performance between and within subjects. SP latency, the size of the corrective saccades and the quality of target's tracking vary substantially. Often during ramp stimulus the HOS exhibits a sequence of corrective saccades interspersed by fixations, rather than tracking the target smoothly. Corrective saccades were more frequent for faster moving targets. We hypothesize that this behavior is exhibited due to dot jumps (step part of the stimulus) that occur in between smooth dot movements (ramp part of the stimulus). Participating subjects do not know when the step or ramp part is going to occur and therefore there is tendency to compensate more with saccadic movement even in case of the ramp stimulus. This hypothesis is sup-

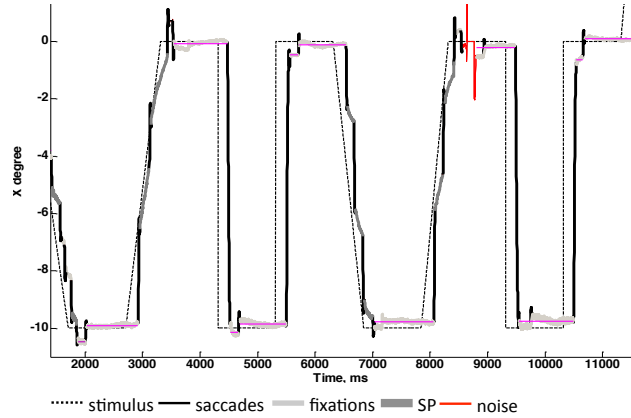


Figure 6. Results of classification performed manually Subject 7 (S7). Only horizontal component of movement is displayed.

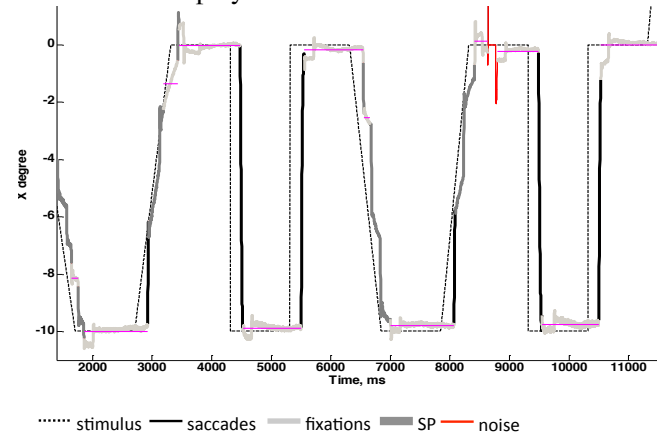


Figure 7. Results of classification performed by I-VDT for Subject 7 (S7). Classification thresholds are selected manually based on classification performance depicted by Figure 5.

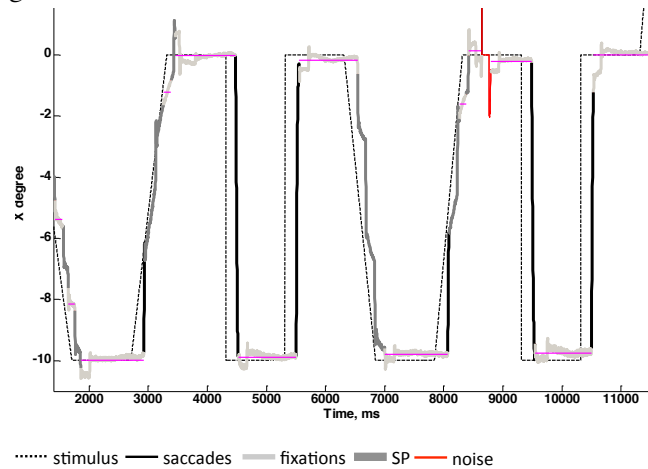


Figure 8. Results of classification performed by I-VDT for Subject 7 (S7). Classification thresholds are selected automatically by proposed objective function (eq. 7).

ported in part by evidence that properties of previous stimulus effect the HOS performance during current task (Collins & Barnes, 2009). Another explanation is possible fatigue due to the fact that stimulus explored here was presented as the last task in a sequence of other tasks, even though the whole sequence of tasks was designed not to cause excessive fatigue. There is evidence, that fatigue might result in excessive presence of corrective saccade during SP stimuli (Bahill et al., 1980). Sometimes closer to the end of the recording, when a subject has experienced a variety of SP stimuli, the HOS started exhibiting during fixational stimulus occasional movements with characteristics resembling the SP even after the termination phase is over. A portion of MisFix errors documented in Table 2 highlight this peculiarity. We have not found any literature that documented similar HOS performance. Such HOS performance further complicates ternary classification and necessitates very careful construction of the ideal behavior scores.

Filter Function

Raw eye positional signal frequently contains jitter and also spikes of noise caused by blinks, equipment slippage, etc. Example of noise can be seen as red spikes in Figure 6, which are observable during the 8-9 s. of the recording. It is important to filter out such events to exclude their impact on signal classification and computation of the behavior scores. “Filter Function” presented in the pseudocodes of the algorithms described earlier performs this role. Automated detection of proper noise events is difficult. Therefore in our implementation of the “Filter Function” we filter out events initially classified as saccades, but which are too short to be actual saccades. A duration threshold of 4ms. is employed for these purposes. In addition all saccades

with amplitude of less than $3.5^{\circ 3}$ are marked for the re-classification to become part of the fixation, SP, or noise. This is done to prevent actual fixation or pursuit signal to be broken into a sequence of disconnected pseudo-saccades, which might occur for the signal recorded at such high temporal sampling rate if this amplitude threshold is lowered. The stability of the fixation/SP detection and noise might come at a price of filtering out actual micro saccades and corrective saccades of small amplitudes. Additional research is necessary for filtering tools that would accurately remove noise while keeping actual miniature eye movements intact.

In our setup those empirically selected thresholds for the amplitude and duration allowed to obtain reasonable automated classification performance, however other experimental setups might require adjustment of the filtering mechanisms and associate thresholds.

It should be noted that during manual classification noise related events are easier to identify due to complete overview of the waveform of the signal. Further research has to be conducted to investigate the impact of the filtering thresholds on classification performance and behavior scores for various types of the experimental setup.

Limitations of the Study

A very specific hardware and step-ramp stimulus was employed in this work to establish a baseline on a high accuracy, high sampling frequency eye tracker. A chin rest was employed for additional stability of the recorded data. Additional research is necessary to provide more comprehensive performance picture of ternary eye movement classification algorithms that employs different hardware, allows freedom of head movement, and contains different stimuli characteristics. We expect that proposed behavior scores would be helpful for assessment of auto-

³ Please note that 3.5° represents 2D amplitude of movement, which makes size of the filtered horizontal and vertical components of movement much smaller.

mated classification performance however careful consideration should be given to the calibration stimulus, types of subject groups used for the recording, and recording environment variables.

CONCLUSIONS

This paper considered and introduced methods for reliable automated ternary classification that consists of three eye movement types: fixations, saccades, and smooth pursuit. This task is extremely challenging due to the substantial variability of Oculomotor system performance between and within subjects, difficulties in separation of fixations from smooth pursuit, and substantial noisiness of the eye tracking data.

We have extended the set of behavior scores originally introduced by Komogortsev and colleagues (Komogortsev et al., 2010) with a purpose of assessing the meaningfulness of ternary classification. Ideal scores values were estimated and additional baseline in a form of manually classified data of various quality was established.

Our findings indicate that a simple extension of the popular velocity threshold method (I-VT) algorithm with an idea of separating fixations from smooth pursuit with an auxiliary velocity threshold will not provide meaningful ternary classification. Two additional algorithms were considered Velocity Movement Pattern Identification (I-VMP) as introduced by San Agustin (Agustin, 2009) and Larsson (2010) and the algorithm that we have developed in this work Velocity Dispersion Threshold Identification (I-VDT). Both algorithms when driven by the optimal thresholds were able to provide classification results that were close to the results obtained via manual classification. However, within considered threshold intervals the I-VDT had smaller performance variability and dependence on the thresholds than the I-VMP possibly indicating

higher practical usefulness. Misclassification errors were also slightly smaller for the proposed I-VDT algorithm. Classification speed is linear for both algorithms.

It was possible to automatically select classification thresholds with an objective function based on the ideal behavior scores to ensure meaningful classification for all algorithms except I-VVT for which accurate identification of fixations and SP is impossible. Such automated threshold selection method should be particularly useful for eye tracking practitioners that would be able to use suggested thresholds for a variety of stimuli recorded immediately after the calibration procedure.

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