Ch 8. Searching and Sorting Arrays 8.1 and 8.3 only

CS 2308 Spring 2013

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Definitions of Search and Sort

- <u>Search</u>: find an item in an array, return the index to the item, or -1 if not found.
- <u>Sort</u>: rearrange the items in an array into some order (smallest to biggest, alphabetical order, etc.).

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- There are various methods (algorithms) for carrying out these common tasks.
- Which ones are better? Why?

Linear Search

- Very simple method.
- Compare first element to target value, if not found then compare second element to target value . . .
- Repeat until: target value is found (return its index) or we run out of items (return -1).

Linear Search in C++

int searchList (int list[], int numElems, int value) {

<pre>int index=0; int position = -1;</pre>	
<pre>bool found = false;</pre>	<pre>//flag, true when value is found</pre>
<pre>while (index < numEler {</pre>	ns && !found)
if (list[index] == v	value) //found the value!
<pre>found = true; position = index;</pre>	<pre>//set the flag //record which item</pre>
<pre>} index++;</pre>	//increment loop index
} return position;	
}	
	What if we don't use found? 4

Program using Linear Search

```
#include <iostream>
using namespace std;
int searchList(int[], int, int);
int main() {
  const int SIZE=5:
  int idNums[SIZE] = {871, 750, 988, 100, 822};
  int results, id;
  cout << "Enter the employee ID to search for: ";
  cin >> id;
  results = searchList(idNums, SIZE, id);
  if (results == -1) {
    cout << "That id number is not registered\n";</pre>
  } else {
    cout << "That id number is found at location ";
    cout << results+1 << endl;</pre>
  3
  return 0:
```

Evaluating the Algorithm

- Is it efficient? Does it do any unnecessary work?
- We measure efficiency of algorithms in terms of number of main steps required to finish.
- For search algorithms, the main step is comparing an array element to the target value.
- Number of steps depends on:
 - size of input array
 - whether or not value is in array
 - where the value is in the array

Efficiency of Linear Search

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	N=50,000	In terms of N
Best Case:	1	1
Average Case:	25,000	N/2
Worst Case:	50,000	Ν

*N is the number of elements in the array

Note: if we search for items not in the array, the average case will increase.

Binary Search

- Works only for SORTED arrays
- Divide and conquer style algorithm
- Compare target value to middle element in list.
 - if equal, then return its index
 - if less than middle element, search in first half of list (repeat)
 - if greater than middle element, search in last half of list (repeat)
- If current search list is narrowed down to 0 elements, return -1

Displacing Cost of Cost of

Binary Search in C++

int binarySearch (int array[], int numElems, int value) {

<pre>last = numElems - 1, //ind</pre>	ex of middle elem ex of target value
while (first <= last && !found)	{
<pre>middle = (first + last) /2;</pre>	//calculate midpoint
<pre>if (array[middle] == value) { found = true; residults</pre>	What if first + last is odd? What if first==last?
<pre>position = middle; } else if (array[middle] > va last = middle - 1; </pre>	
<pre>} else { first = middle + 1;</pre>	//search upper half
} } return position; }	10

Binary Search Example Exam Question!

The target of your search is 42. Given the following list of integers, record the values of first, last, and middle during a binary search. Assume the following numbers are in an array.

1 7 8 14 20 42 55 67 78 101 112 122 170 179 190

Repeat the exercise with a target of 82

first	0	0	4	first		8		
last	14	6	6	last	14	14	10	8
middle	7	3	5	middle	7	11	9	8

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Note: these are the **indexes**, not the values in the array

Program using Binary Search

```
#include <iostream>
using namespace std;
                                             How is this program different
int binarySearch(int[], int, int);
                                             from the one on slide 5?
int main() {
  const int SIZE=5;
  int idNums[SIZE] = {100, 750, 822, 871, 988};
  int results, id;
  cout << "Enter the employee ID to search for: ";
  cin >> id;
  results = binarySearch(idNums, SIZE, id);
  if (results == -1) {
    cout << "That id number is not registered\n";</pre>
  } else {
    cout << "That id number is found at location ";
    cout << results+1 << endl;</pre>
  }
                                                          12
  return 0;
```

Ef	ficiency of E	Binary Sear	rch
	Calculate worst c	ase for N=1024	
[Items left to search	Comparisons so far]
	1024	0	
[512	1	
	256	2	
	128	3	
	64	4	
	32	5	
	16	6	
	8	7	
	4	8	
	2	9	Goal: calculate
	1	10 +	this value from N
	1024 = 2 ¹⁰ <==:	> log ₂ 1024 = 10	

Efficiency of Binary Search

If N is the number of elements in the array, how many comparisons (steps)?

1024 = 21	¹⁰ <==> lo	og ₂ 1024 = 10	
N = 2 ^{steps}	<==> log	$_2$ N = steps	To what power do I raise 2 to get N?
	N=50,000	In terms of N	
Best Case:	1	1	
Worst Case:	16	log ₂ N	Rounded up to next whole number

Is Log₂N better than N?

Is <u>binary search</u> better than <u>linear search</u>?

Compare values of N/2, N, and Log₂ N as N increases:

Is this really a fair comparison?

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Ν	N/2	Log ₂ N
5	2.5	2.3
50	25	5.6
500	250	9.0
5,000	2,500	12.3
50,000	25,000	15.6

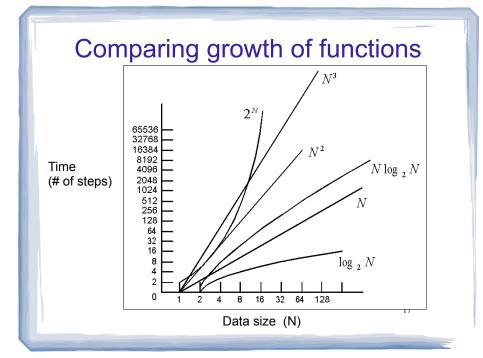
N and N/2 are growing much faster than log N!

slower growing is more efficient (fewer steps).

Classifications of (math) functions

Constant	f(x)=b	O(1)
Logarithmic	$f(x)=log_b(x)$	O(log n)
Linear	f(x)=ax+b	O(n)
Linearithmic	$f(x)=x \log_{b}(x)$	O(n log n)
Quadratic	f(x)=ax ² +bx+c	O(n²)
Exponential	f(x)=b ^x	O(2 ⁿ)

- Last column is "big Oh notation", used in CS.
- It ignores all but dominant term, constant factors



Efficiency of Algorithms

- To classify efficiency of an algorithm:
 - Express "time" (using number of main steps or comparisons), as a function of input size
 - Determine which classification the function fits into.

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• Nearer to the top of the chart is slower growth, and more efficient (constant is better than logarithmic, etc.)

8.3 Sorting Algorithms

- Sort: rearrange the items in an array into ascending or descending order.
- Selection Sort
- Bubble Sort



 55
 112
 78
 14
 20
 179
 42
 67
 190
 7
 101
 1
 122
 170
 8
 unsorted

 1
 7
 8
 14
 20
 42
 55
 67
 78
 101
 112
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 179
 190
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 sorted

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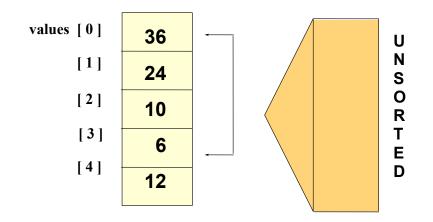
Why is sorting important?

- Searching in a sorted list is much easier than searching in an unsorted list.
- Especially for people
 - dictionary entries
 - phone book
 - card catalog in library
 - bank statement: transactions in date order
- Most of the data displayed by computers is sorted.

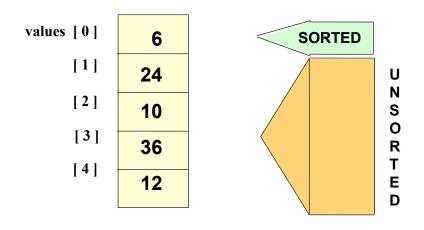
Selection Sort

- There is a pass for each position (0..size-1)
- On each pass, the smallest (minimum) element in the rest of the list is exchanged (swapped) with element at the current position.
- The first part of the list (the part that is already processed) is always sorted
- Each pass increases the size of the sorted portion.

Selection Sort: Pass One

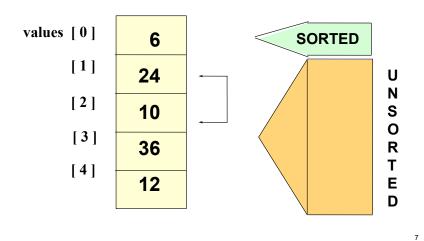


Selection Sort: End Pass One

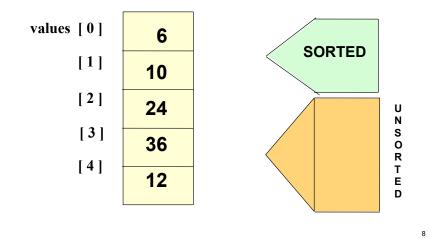


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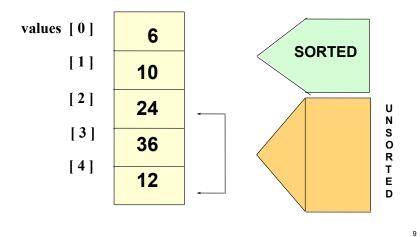
Selection Sort: Pass Two



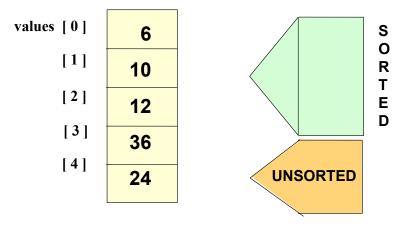
Selection Sort: End Pass Two



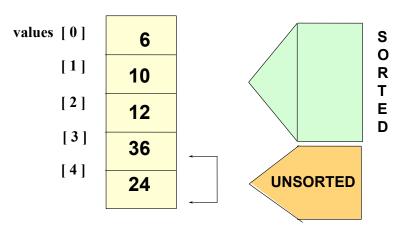
Selection Sort: Pass Three

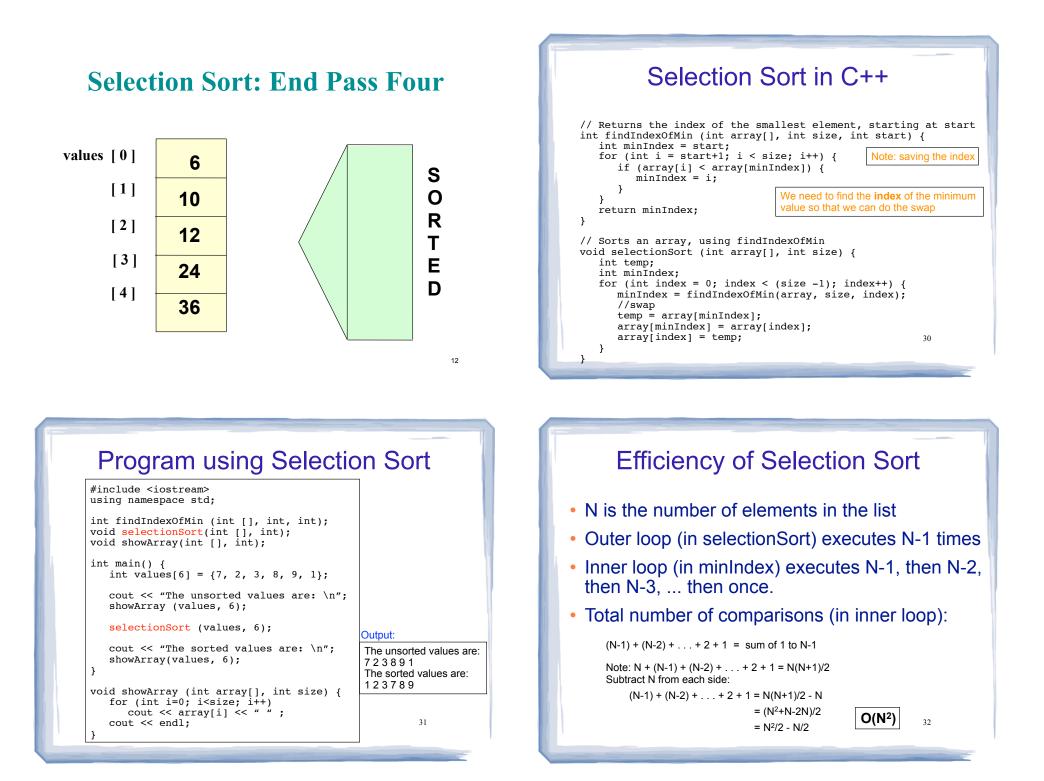


Selection Sort: End Pass Three



Selection Sort: Pass Four





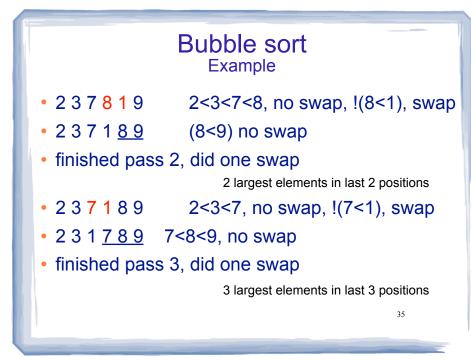
The Bubble Sort

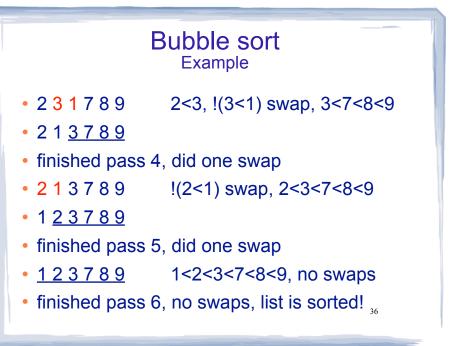
- On each pass:
 - Compare first two elements. If the first is bigger, they exchange places (swap).
 - Compare second and third elements. If second is bigger, exchange them.
 - Repeat until last two elements of the list are compared.
- Repeat this process until a pass completes with no exchanges

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Bubble sort Example • 7 2 3 8 9 1 7 > 2, swap • 2 7 3 8 9 1 7 > 3, swap • 2 3 7 8 9 1 !(7 > 8), no swap • 2 3 7 8 9 1 !(8 > 9), no swap • 2 3 7 8 9 1 9 > 1, swap • 2 3 7 8 1 9 finished pass 1, did 3 swaps

Note: largest element is in last position





Bubble sort how does it work?

- At the end of the first pass, the largest element is moved to the end (it's bigger than all its neighbors)
- At the end of the second pass, the second largest element is moved to just before the last element.
- The back end (tail) of the list remains sorted.
- Each pass increases the size of the sorted portion.
- No exchanges implies each element is smaller than its next neighbor (so the list is sorted).

Bubble Sort in C++

	ol swap; t temp;
do	{
	<pre>swap = false; for (int i = 0; i < (size-1); i++) {</pre>
	if (array [i] > array[i+1]) {
	<pre>temp = array[i]; array[i] = array[i+1]; array[i+1] = temp; swap = true;</pre>
	}
7 {	while (swap);

