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- Very simple method.
- Compare first element to target value, if not found then compare second element to target value . . .

3

Repeat until: target value is found (return its index) or we run out of items (return -1).

Linear Search in C++
<pre>int searchList (int list[], int size, int target) {</pre>
<pre>int position = -1; //position of target</pre>
<pre>for (int i=0; i<size; (list[i]="target)" found="" i++)="" if="" item="" position="i;" position;="" pre="" record="" return="" target!="" the="" which="" {="" }="" }<=""></size;></pre>
Is this algorithm correct?
Is this algorithm efficient (or does it do unnecessary work)?
4



# Program that uses linear search

```
#include <iostream>
using namespace std;
int searchList(int[], int, int);
int main() {
   const int SIZE=5;
   int idNums[SIZE] = {871, 750, 988, 100, 822};
   int results, id;
   cout << "Enter the employee ID to search for: ";
   cin >> id;
   results = searchList(idNums, SIZE, id);
   if (results == -1) {
      cout << "That id number is not registered\n";
    } else {
      cout << "That id number is found at location ";
      cout << results+1 << endl;
   }
}</pre>
```

# Evaluating the Algorithm

- Does it do any unnecessary work?
- Is it efficient? How would we know?
- We measure efficiency of algorithms in terms of number of main steps required to finish.
- For search algorithms, the main step is comparing an array element to the target value.
- Number of steps depends on:
  - size of input array
  - whether or not value is in array
  - where the value is in the array

#### Efficiency of Linear Search how many steps?

N is the number of elements in the array

	N=50,000	In terms of N
Best Case:	1	1
Average Case:	25,000	N/2
Worst Case:	50,000	Ν

Note: if we search for many items that are not in the array, the average case result will increase.

### **Binary Search**

- Works only for SORTED arrays
- Divide and conquer style algorithm
- Compare target value to middle element in list.
  - if equal, then return its index
  - if less than middle element, repeat the search in the first half of list
  - if greater than middle element, repeat the search in last half of list
- If current search list is narrowed down to 0 elements, return -1

# Binary Search Algorithm

#### • The algorithm described in pseudocode:

while (number of items in list >= 1)

if (item at middle position is equal to target) target is found! End of algorithm else

if (target < middle item) list = lower half of list else

(narrow search list)

list = upper half of list

end while

if we reach this point: target not found

10



#### Binary Search in C++ int binarySearch (int array[], int size, int target) { //index to (current) first elem int first = 0, last = size -1. //index to (current) last elem middle, //index of (current) middle elem //index of target value position = -1;bool found = false: //flag while (first <= last && !found) { middle = (first + last) /2; //calculate midpoint What if first + last is odd? if (array[middle] == target) { found = true; What if first==last? position = middle: } else if (target < array[middle]) {</pre> last = middle - 1; //search lower half else { first = middle + 1; //search upper half return position; 12 3

#### Binary Search Example Exam Question!

The target of your search is 42. Given the following list of integers, record the values stored in the variables named first, last, and middle during a binary search. Assume the following numbers are in an array.

values:	1	7	8	14	20	42	55	67	78	101	112	122	170	179	190
indexes:	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

Repeat the exercise with a target of 82

0 0 4	first 0 8 8 8 9
14 6 6	last 14 14 10 8 8
2 7 3 5	middle 7 11 9 8

Note: these are the indexes, not the values in the array

# Program using Binary Search

#include <iostream>
using namespace std;

}

int binarySearch(int[], int, int); int main() { const int SIZE=5; int idNums[SIZE] = {100, 750, 822, 871, 988}; int results, id; cout << "Enter the employee ID to search for: "; cin >> id;

results = binarySearch(idNums, SIZE, id);

- if (results == -1) {
   cout << "That id number is not registered\n";
  } else {
   cout << "That id number is found at location ";</pre>
- cout << results+1 << endl;

### Efficiency of Binary Search

#### Calculate worst case for N=1024

Items left to search	Comparisons so far	
1024	0	
512	1	
256	2	
128	3	
64	4	
32	5	
16	6	
8	7	
4	8	
2	9	Goal: calculate
1	10 +	this value from
1024 = 2 <sup>10</sup> <==	> log <sub>2</sub> 1024 = 10	

# Efficiency of Binary Search

If N is the number of elements in the array, how many comparisons (steps)?

	1024 = 21	<sup>10</sup> <==> lo	og <sub>2</sub> 1024 = 10	
	N = 2 <sup>steps</sup>	To what power do I raise 2 to get N?		
		N=50,000	In terms of N	
В	est	1	1	
C	ase:			
W	/orst	16	log <sub>2</sub> N 🐛	Rounded up to
С	ase:			number

# Is Log<sub>2</sub>N better than N?

Is binary search better than linear search?

Is this really a fair comparison?

Compare values of N/2, N, and  $Log_2$  N as N increases:

N	N/2	Log <sub>2</sub> N
5	2.5	2.3
50	25	5.6
500	250	9.0
5,000	2,500	12.3
50,000	25,000	15.6

N and N/2 are growing much faster than log N!

slower growing is more efficient (fewer steps).

# Classifications of (math) functions

Constant	f(x)=b	O(1)
Logarithmic	$f(x)=log_b(x)$	O(log n)
Linear	f(x)=ax+b	O(n)
Linearithmic	$f(x)=x \log_b(x)$	O(n log n)
Quadratic	f(x)=ax <sup>2</sup> +bx+c	O(n <sup>2</sup> )
Exponential	f(x)=b <sup>x</sup>	O(2 <sup>n</sup> )

- Last column is "big Oh notation", used in CS.
- It ignores all but dominant term, constant factors



# Efficiency of Algorithms

- To classify the efficiency of an algorithm:
  - Express "time" (using number of main steps or comparisons), as a function of input size
  - Determine which classification the function fits into.
- Nearer to the top of the chart is slower growth, and more efficient (constant is better than logarithmic, etc.)

# 8.3 Sorting Algorithms

- Sort: rearrange the items in an array into ascending or descending order.
- Selection Sort
- Bubble Sort



 55
 112
 78
 14
 20
 179
 42
 67
 190
 7
 101
 1
 122
 170
 8
 unsorted

 1
 7
 8
 14
 20
 42
 55
 67
 78
 101
 112
 122
 170
 179
 190
 ,, sorted

# Why is sorting important?

- Searching in a sorted list is much easier than searching in an unsorted list.
- Especially for people:
  - dictionary entries (in a dictionary book)
  - phone book (remember these?)
  - card catalog in library (it used to be drawers of index cards)
  - bank statement: transactions in date order
- Most of the data displayed by computers<sub>22</sub> is sorted.

# **Selection Sort**

- There is a pass for each position (0..size-1)
- On each pass, the smallest (minimum) element in the rest of the list is exchanged (swapped) with element at the current position.
- The first part of the list (the part that is already processed) is always sorted
- Each pass increases the size of the sorted portion.

# **Selection Sort: Pass One**



5

# **Selection Sort: End Pass One**



### **Selection Sort: Pass Two**



# **Selection Sort: End Pass Two**



8

# **Selection Sort: Pass Three**



### **Selection Sort: End Pass Three**



### **Selection Sort: Pass Four**



**Selection Sort: End Pass Four** 







# Efficiency of Selection Sort

- N is the number of elements in the list.
- Outer loop (in selectionSort) executes N-1 times
- Inner loop (in minIndex) executes N-1, then N-2, then N-3, ... then once.
- Total number of comparisons (in inner loop):

(N-1) + (N-2) + ... + 2 + 1 = sum of 1 to N-1

Note: N + (N-1) + (N-2) + . . . + 2 + 1 = N(N+1)/2Subtract N from each side: (N-1) + (N-2) + ... + 2 + 1 = N(N+1)/2 - N $= (N^{2}+N)/2 - 2N/2$ 0  $= (N^{2}+N-2N)/2$ = N<sup>2</sup>/2 - N/2

)(N <sup>2</sup> )	34



Bubble sort Example			
• 2 3 7 8 1 9 2<3<7<8, no swap, !(8<1), swap			
• 2 3 7 1 <u>8 9</u> (8<9) no swap			
<ul> <li>finished pass 2, did one swap</li> </ul>			
2 largest elements in last 2 positions			
• 2 3 7 1 8 9 2<3<7, no swap, !(7<1), swap			
• 2 3 1 <u>7 8 9</u> 7<8<9, no swap			
<ul> <li>finished pass 3, did one swap</li> </ul>			
3 largest elements in last 3 positions			
37			



#### Bubble sort how does it work?

- At the end of the first pass, the largest element is moved to the end (it's bigger than all its neighbors)
- At the end of the second pass, the second largest element is moved to just before the last element.
- The back end (tail) of the list remains sorted.
- Each pass increases the size of the sorted portion.
- No exchanges implies each element is smaller than its next neighbor (so the list is sorted).

# Bubble Sort in C++



